

# Package ‘CombinS’

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**Type** Package

**Title** Construction Methods for Series of PBIB Designs via Combinatory Method S

**Version** 1.2

**Date** 2025-05-27

**Description** Provides constructions of series of partially balanced incomplete block designs (PBIB) based on the combinatory method S, introduced by Rezgui et al. (2014) <[doi:10.3844/jmssp.2014.45.48](https://doi.org/10.3844/jmssp.2014.45.48)>. This package also offers the associated U-type designs. Version 1.1-1 generalizes the approach to designs with  $v = w$  treatments. It includes various rectangular and generalized rectangular right angular association schemes with 4, 5, and 7 associated classes.

**Imports** stats, utils

**URL** <https://mlaib.net>

**License** GPL-3

**Encoding** UTF-8

**RoxygenNote** 7.3.2

**NeedsCompilation** no

**Author** Mohamed Laib [aut, cre],  
Imane Rezgui [aut],  
Zebida Gheribi-Aoulmi [aut],  
Herve Monod [aut]

**Maintainer** Mohamed Laib <[laib.med@gmail.com](mailto:laib.med@gmail.com)>

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Combs	<i>The Combinatory Method (s) for the construction of rectangular PBIB designs</i>
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### Description

The application of the Combinatory Method (s), with  $s$  chosen in  $[2, l-1]$ , on rectangular association scheme to obtain the configuration and the parameters of the PBIB design associated.

### Usage

Combs(n, l, s)

### Arguments

n	Number of lines of the association schemes array.
l	Number of columns of the association schemes array.
s	Number of the token treatments from the same row of the association scheme.

### Details

- For  $2 < s < l$ , we obtain a rectangular PBIB design.
- For  $s = l$ , we obtain a singular group divisible designs.

### Value

A LIST :

- PBIB The configuration of the PBIB.
- Type The type of the design
- V Number of treatments.
- B Number of blocs.
- R Repetition of each treatment.
- K Size of blocs.
- lamda Vector of m-lambda.
- Resolvable Is the design Resolvable ?

### Author(s)

Mohamed Laib, Imane Rezgui, Zebida Gheribi-Aoulmi and Herve Monod

## References

Imane Rezgui, Z. Gheribi-Aoulmi (2014). New construction method of rectangular partially balanced incomplete block designs and singular group divisible designs, Journal of Mathematics and Statistics, 10, 45- 48.

M.N. Vartak 1955. On an application of Kronecker product of Matrices to Statistical designs. Ann. Math. Stat.,26(420-438).

## See Also

[UType](#)

## Examples

```
## Not run:
n<-3
l<-3
s<-2
CombS(l,n,s)

## End(Not run)
```

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GPBIB4A

*Generalized rectangular right angular (4) design with  $\lambda_4 = 0$*

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## Description

Gives the configuration and the parametres of the design obtained by the first construction method of GPBIB\_4 (see 3.1.1 of the paper rezgui et al (2015)).

## Usage

```
GPBIB4A(n, l, s, w)
```

## Arguments

n	Number of lines of the association schemes array.
l	Number of columns of the association schemes array.
s	Number of the token treatments from the same row of the association scheme.
w	Number of the association scheme arrays.

## Details

- For  $s = l$ , the previous method gives configuration of nested group divisible designs.

**Value**

A LIST :

- PBIB The configuration of the PBIB.
- Type The type of the design
- V Number of treatments.
- B Number of blocs.
- R Repetition of each treatment.
- K Size of blocs.
- lamda Vector of m-lambda.
- Resolvable Is the design Resolvable ?

**Note**

For  $w = 2$ , the GPBIB\_4 is a rectangular right angular (4) (PBIB\_4)

**Author(s)**

Mohamed Laib, Imane Rezgui, Zebida Gheribi-Aoulmi and Herve Monod

**References**

Imane Rezgui, Z. Gheribi-Aoulmi and H. Monod (2015). U-type Designs via New Generalized Partially Balanced Incomplete Block Designs with  $m = 4, 5$  and  $7$  Associated Classes, [doi:10.4236/am.2015.62024](https://doi.org/10.4236/am.2015.62024), Applied mathematics, 6, 242-264.

Imane Rezgui, Z.Gheribi-Aoulmi and H. Monod, New association schemes with  $4, 5$  and  $7$  associated classes and their associated partially balanced incomplete block designs; Advances and Applications in Discrete Mathematics Vol.12 Issue 2 197-206.

**See Also**

[GPBIB4B](#) and [UType](#)

**Examples**

```
## Not run:
n<-3
l<-3
s<-3
w<-3
GPBIB4A(n, l, s, w)

## End(Not run)
```

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GPBIB4B	<i>Generalized rectangular right angular (4) design with <math>\lambda_4</math> not equal to 0</i>
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### Description

Gives the configuration and the parametres of the design obtained by the seconde construction method of GPBIB\_4 (see 3.1.2 of the paper rezgui et al (2015)).

### Usage

GPBIB4B(n, l, s, w)

### Arguments

n	Number of lines of the association schemes array.
l	Number of columns of the association schemes array.
s	Number of the token treatments from the same row of the association scheme.
w	Number of the association scheme arrays.

### Value

A LIST :

- PBIB The configuration of the PBIB.
- Type The type of the design
- V Number of treatments.
- B Number of blocs.
- R Repetition of each treatment.
- K Size of blocs.
- lamda Vector of m-lambda.
- Resolvable Is the design Resolvable ?

### Note

For  $w = 2$ , the GPBIB\_4 is a rectangular right angular (4) (PBIB\_4)

### Author(s)

Mohamed Laib, Imane Rezgui, Zebida Gheribi-Aoulmi and Herve Monod

References

Imane Rezgui, Z. Gheribi-Aoulmi and H. Monod (2015). U-type Designs via New Generalized Partially Balanced Incomplete Block Designs with  $m = 4, 5$  and  $7$  Associated Classes, [doi:10.4236/am.2015.62024](#), Applied mathematics, 6, 242-264.

Imane Rezgui, Z.Gheribi-Aoulmi and H. Monod, New association schemes with  $4, 5$  and  $7$  associated classes and their associated partially balanced incomplete block designs; Advances and Applications in Discrete Mathematics Vol.12 Issue 2 197-206.

See Also

[GPBIB4A](#) and [UType](#)

Examples

```
## Not run:
n<-3
l<-3
s<-3
w<-3
GPBIB4B(n, l, s, w)

## End(Not run)
```

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GPBIB5	<i>Generalized rectangular right angular (5) design.</i>
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Description

gives the configuration and the parametres of the design obtained by the construction method of GPBIB\_5 (see 3.2 of the paper rezgui et al (2015)).

Usage

```
GPBIB5(n, l, s, w)
```

Arguments

- |   |   |
|---|---|
| n | Number of lines of the association schemes array.                           |
| l | Number of columns of the association schemes array.                         |
| s | Number of the token treatments from the same row of the association scheme. |
| w | Number of the association scheme arrays.                                    |

**Value**

A LIST :

- PBIB The configuration of the PBIB.
- Type The type of the design
- V Number of treatments.
- B Number of blocs.
- R Repetition of each treatment.
- K Size of blocs.
- lamda Vector of m-lambda.
- Resolvable Is the design Resolvable ?

**Note**

For  $w = 2$ , the GPBIB\_5 is a rectangular right angular (5) (PBIB\_5).

**Author(s)**

Mohamed Laib, Imane Rezgui, Zebida Gheribi-Aoulmi and Herve Monod

**References**

Imane Rezgui, Z. Gheribi-Aoulmi and H. Monod (2015). U-type Designs via New Generalized Partially Balanced Incomplete Block Designs with  $m = 4, 5$  and  $7$  Associated Classes, [doi:10.4236/am.2015.62024](https://doi.org/10.4236/am.2015.62024), Applied mathematics, 6, 242-264.

Imane Rezgui, Z.Gheribi-Aoulmi and H. Monod, New association schemes with 4, 5 and 7 associated classes and their associated partially balanced incomplete block designs; Advances and Applications in Discrete Mathematics Vol.12 Issue 2 197-206.

**See Also**

[UType](#)

**Examples**

```
## Not run:
n<-3
l<-3
s<-3
w<-3
GPBIB5(n, l, s, w)

## End(Not run)
```

---

GPBIB7A	<i>Generalized rectangular right angular (7) design with <math>\lambda_i</math> equal to <math>\lambda_i + 4</math> (<math>i = 1, \dots, 4</math>)</i>
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### Description

gives the configuration and the parametres of the design obtained by the first construction method of GPBIB\_7 (see 3.3.1 of the paper rezgui et al (2015))

### Usage

GPBIB7A(n, l, s, w)

### Arguments

n	Number of lines of the association schemes array.
l	Number of columns of the association schemes array.
s	Number of the token treatments from the same row of the association scheme.
w	Number of the association scheme arrays.

### Value

A LIST :

- PBIB The configuration of the PBIB.
- Type The type of the design
- V Number of treatments.
- B Number of blocs.
- R Repetition of each treatment.
- K Size of blocs.
- lambda Vector of m-lambda.
- Resolvable Is the design Resolvable ?

### Note

For  $w = 2$ , the GPBIB\_7 is a rectangular right angular (7) (PBIB\_7).

### Author(s)

Mohamed Laib, Imane Rezgui, Zebida Gheribi-Aoulmi and Herve Monod



References

Imane Rezgui, Z. Gheribi-Aoulmi and H. Monod (2015). U-type Designs via New Generalized Partially Balanced Incomplete Block Designs with  $m = 4, 5$  and  $7$  Associated Classes, [doi:10.4236/am.2015.62024](https://doi.org/10.4236/am.2015.62024), Applied mathematics, 6, 242-264.

Imane Rezgui, Z.Gheribi-Aoulmi and H. Monod, New association schemes with  $4, 5$  and  $7$  associated classes and their associated partially balanced incomplete block designs; Advances and Applications in Discrete Mathematics Vol.12 Issue 2 197-206.

See Also

[GPBIB7B](#) and [UType](#)

Examples

```
## Not run:
n<-3
l<-3
s<-3
w<-3
GPBIB7A(n, l, s, w)

## End(Not run)
```

---

GPBIB7B	<i>Generalized rectangular right angular (7) design with distinct <math>\lambda_i</math> (<math>i=1,...,7</math>)</i>
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Description

Gives the configuration and the parametres of the design obtained by the seconde construction method of GPBIB\_7 (see 3.3.2 of the paper rezgui et al (2015)).

Usage

```
GPBIB7B(n, l, s, w)
```

Arguments

- n                      Number of lines of the association schemes array.
- l                      Number of columns of the association schemes array.
- s                      Number of the token treatments from the same row of the association scheme.
- w                      Number of the association scheme arrays.

**Value**

A LIST :

- PBIB The configuration of the PBIB.
- Type The type of the design
- V Number of treatments.
- B Number of blocs.
- R Repetition of each treatment.
- K Size of blocs.
- lambda Vector of m-lambda.
- Resolvable Is the design Resolvable ?

**Note**

For  $w = 2$ , the GPBIB\_7 is a rectangular right angular (7) (PBIB\_7).

**Author(s)**

Mohamed Laib, Imane Rezgui, Zebida Gheribi-Aoulmi and Herve Monod

**References**

Imane Rezgui, Z. Gheribi-Aoulmi and H. Monod (2015). U-type Designs via New Generalized Partially Balanced Incomplete Block Designs with  $m = 4, 5$  and  $7$  Associated Classes, [doi:10.4236/am.2015.62024](https://doi.org/10.4236/am.2015.62024), Applied mathematics, 6, 242-264.

Imane Rezgui, Z.Gheribi-Aoulmi and H. Monod, New association schemes with 4, 5 and 7 associated classes and their associated partially balanced incomplete block designs; Advances and Applications in Discrete Mathematics Vol.12 Issue 2 197-206.

**See Also**

[GPBIB7A](#) and [UType](#)

**Examples**

```
## Not run:
n<-3
l<-3
s<-3
w<-3
GPBIB7B(n, l, s, w)

## End(Not run)
```

---

UType

*U-type design via some PBIB designs*


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**Description**

Applies the Fang algorithm on our constructed designs to obtain the configuration and the parameters of the U-type design associated.

**Usage**

```
UType(lst)
```

**Arguments**

lst                      The output of one of our package functions.

**Value**

A LIST :

- v Number of runs.
- r Number of factors.
- UtypeDesign The configuration of the U-type design..

**Author(s)**

Mohamed Laib, Imane Rezgui, Zebida Gheribi-Aoulmi and Herve Monod

**References**

K.T. Fang, R.Li and A.Sudjanto (2006). Design ans Modeling for Computer Experiments. Taylor & Francis Group, LLC London.

**Examples**

```
## Not run:
M<-GPBIB4A(4,4,2,2)
UType(M)

## End(Not run)
```

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