# Package 'MaxPro'

July 21, 2025

Type Package

Title Maximum Projection Designs

Version 4.1-2
<b>Date</b> 2018-09-27
Author Shan Ba and V. Roshan Joseph
Maintainer Shan Ba <shanbatr@gmail.com></shanbatr@gmail.com>
Depends nloptr
Description Generate maximum projection (MaxPro) designs for quantitative and/or qualitative factors. Details of the MaxPro criterion can be found in: (1) Joseph, Gul, and Ba. (2015) ``Maximum Projection Designs for Computer Experiments", Biometrika, 102, 371-380, and (2) Joseph, Gul, and Ba. (2018) ``Designing Computer Experiments with Multiple Types of Factors: The MaxPro Approach", Journal of Quality Technology, to appear.
License LGPL-2.1
NeedsCompilation yes
Repository CRAN
<b>Date/Publication</b> 2018-09-28 04:40:03 UTC
Contents
MaxPro-package       2         CandPoints       3         MaxPro       4         MaxProAugment       5         MaxProLHD       7         MaxProMeasure       8         MaxProQQ       9         MaxProRunOrder       11
Index 14

2 MaxPro-package

MaxPro-package MaxPro package

## Description

Maximum projection (MaxPro) designs for quantitative and/or qualitative factors

#### **Details**

Package: MaxPro
Type: Package
Version: 4.1-2
Date: 2018-09-27
License: LGPL-2.1

Important functions in this package are: MaxProLHD generates the MaxPro Latin hypercube design for continuous factors, MaxPro searches for the locally optimal MaxPro design in the neighborhood of a given initial design for continuous factors, MaxProQQ generates the MaxPro design with both quantitative and qualitative factors, MaxProAugment sequentially augments an existing design with additional design points based on the MaxPro criterion for all types of factors and constraints, MaxProRunOrder finds the optimal order to run a given design in a sequential manner based on the MaxPro criterion, and MaxProMeasure reports the MaxPro criterion value for a given design.

#### Author(s)

Shan Ba and V. Roshan Joseph

Maintainer: Shan Ba <shanbatr@gmail.com>

#### References

Joseph, V. R., Gul, E., and Ba, S. (2015) "Maximum Projection Designs for Computer Experiments," *Biometrika*, 102, 371-380.

Joseph, V. R., Gul, E., and Ba, S. (2018) "Designing Computer Experiments with Multiple Types of Factors: The MaxPro Approach," *Journal of Quality Technology*, to appear.

CandPoints 3

CandPoints	Generate Candidate Design Points Randomly for Various Types of Factors
------------	--

## Description

Quickly generate random candidate design points for different types of factors which can be used as an input to the MaxProAugment function.

#### Usage

```
CandPoints(N,p_cont,l_disnum=NULL,l_nom=NULL)
```

## Arguments

N	The number of random candidate design points to generate
p_cont	The number of continuous factors
l_disnum	Optional, default is "NULL". A vector containing the number of levels for each discrete numeric factor (NULL if there are no discrete numeric factors)
1_nom	Optional, default is "NULL". A vector containing the number of levels for each nominal factor (NULL if there are no nominal factors)

### **Details**

This function generates uniform random numbers for each continuous factor and randomly sampled levels for each discrete numeric and nominal factor. The result can be used as the candidate design in the MaxProAugment function.

#### Value

The value returned from the function is a matrix containing the candidate design points.

## Author(s)

Shan Ba <shanbatr@gmail.com> and V. Roshan Joseph <roshan@isye.gatech.edu>

#### See Also

MaxProAugment

## **Examples**

```
\label{eq:ccc-cand-cont} \mbox{CCC} \leftarrow \mbox{CandPoints} (\mbox{N=10000}, \mbox{p\_cont=3}, \mbox{l\_disnum=c}(3, 3, 4), \mbox{l\_nom=c}(2, 2, 3))
```

4 MaxPro

MaxPro

Locally Optimal Maximum Projection Designs for Continuous Factors

#### **Description**

Find the locally optimal maximum projection (MaxPro) design in the neighborhood of a given initial design for continuous factors.

#### Usage

MaxPro(InitialDesign, s=2, iteration=10)

#### **Arguments**

InitialDesign The initial design matrix, which we recommend to be a MaxPro Latin hypercube

design generated by the MaxProLHD function

s Optional, default is "2". The parameter in defining the s-norm distance (2 cor-

responds to Euclidean distance)

iteration Optional, default is "10". The number of iterations in running the continuous

local search

#### **Details**

This function applies a continuous optimization algorithm in nloptr (Ypma 2014) to find the locally optimal MaxPro design in the neighborhood of the initial design. A MaxPro Latin hypercube design generated by the MaxProLHD function is a good choice for the initial design. Please refer to Joseph, Gul and Ba (2015) for details.

#### Value

The value returned from the function is a list containing the following components:

Design The locally optimal MaxPro design matrix

measure The MaxPro criterion measure for the locally optimal design

#### Author(s)

Shan Ba <shanbatr@gmail.com> and V. Roshan Joseph <roshan@isye.gatech.edu>

#### References

Joseph, V. R., Gul, E., and Ba, S. (2015) "Maximum Projection Designs for Computer Experiments," *Biometrika*, 102, 371-380.

Ypma, J. (2014) "Introduction to nloptr: an R interface to NLopt", R Package Version 1.0.0.

#### See Also

MaxProLHD, MaxProRunOrder, MaxProAugment

MaxProAugment 5

### **Examples**

```
InitialDesign<-MaxProLHD(n = 10, p = 4)$Design
DOX<-MaxPro(InitialDesign)
DOX$Design</pre>
```

MaxProAugment Augment an Existing Design based on the Maximum Projection Criterion

#### **Description**

Select the best set of design points to augment a given design matrix by optimizing the maximum projection (MaxPro) criterion sequentially. When multiple types of factors exist, all continuous factors should be placed as the leftmost columns in the design matrix, discrete numeric factors should be placed as middle columns, and all nominal factors should be placed at the rightmost columns in the design matrix. The ordinal factors, if any, should be pre-converted into discrete numeric factors through the scoring method (see, e.g., Wu and Hamada 2009, Section 14.10). This function can also be used for creating a nonadaptive sequential design, designs to run in batches, validation runs, designs in constrained regions, and nested designs.

#### Usage

```
MaxProAugment(ExistDesign, CandDesign, nNew,
p_disnum=0, l_disnum=NULL, p_nom=0, l_nom=NULL)
```

### **Arguments**

ExistDesign	The existing design matrix to be augmented, where each row is an experimental run and each column is a factor. All columns of the continuous and discrete numeric factors should be standardized into the unit range of $[0,1]$ .
CandDesign	The matrix containing candidate design points, whose columns should match those in the ExistDesign matrix. All columns of the continuous and discrete numeric factors should be standardized into the unit range of [0,1]. Function CandPoints can be used to quickly generate candidate design points.
nNew	The number of new design points to add
p_disnum	Optional, default is 0. The number of discrete numeric factors
l_disnum	Optional, default is a vector containing the number of distinct levels for each discrete numeric factor in the ExistDesign and CandDesign. The vector specifying the number of levels for each discrete numeric factor
p_nom	Optional, default is 0. The number of nominal factors
l_nom	Optional, default is a vector containing the number of levels for each nominal factor in the ExistDesign and CandDesign. The vector specifying the number of levels for each nominal factor

6 MaxProAugment

#### **Details**

This function uses a greedy search algorithm to select the best nNew points out of the CandDesign matrix to augment the ExistDesign matrix based on the MaxPro criterion. Factor constraints (irregular-shaped design space), if any, can be incorporated through the specification of valid candidate design points in CandDesign (please see the example below).

#### Value

The value returned from the function is a list containing the following components:

Design The augmented design matrix (including the original existing design points)

measure The MaxPro criterion measure of the augmented design

time\_rec Time to complete the search

#### Author(s)

Shan Ba <shanbatr@gmail.com> and V. Roshan Joseph <roshan@isye.gatech.edu>

#### References

Joseph, V. R., Gul, E., and Ba, S. (2015) "Maximum Projection Designs for Computer Experiments," *Biometrika*, 102, 371-380.

Joseph, V. R. (2016) "Rejoinder," Quality Engineering, 28, 42-44.

Joseph, V. R., Gul, E., and Ba, S. (2018) "Designing Computer Experiments with Multiple Types of Factors: The MaxPro Approach," *Journal of Quality Technology*, to appear.

Wu, C. F. J., and Hamada, M. (2009), *Experiments: Planning, Analysis, and Parameter Design Optimization*, 2nd Edition, New York: Wiley.

## See Also

CandPoints, MaxProLHD, MaxProQQ

## Examples

```
ExistDesign=matrix(c(0.11,0.96,0.42,0.99),ncol=2,byrow=TRUE)

#Generate candidate design points that satisfy the factor constraints
S=CandPoints(N=10000,p_cont=2)
S=S[S[,1]+S[,2]<=1.5,] #constraint 1
S=S[(S[,1]-.5)^2+(S[,2]-.5)^2>=(2*.25^2),] #constraint 2
plot(S[,1],S[,2],bty="n",cex=.5,xlab=expression(x[1]),ylab=expression(x[2]),xlim=c(0,1),ylim=c(0,1))

result=MaxProAugment(ExistDesign, CandDesign=S, nNew=20)
D=result$Design
points(D[,1],D[,2],col='red',pch=16)
text(D[,1],D[,2],1:nrow(D),col=2,cex=2)
```

MaxProLHD 7

	MaxProLHD	Maximum Projection Latin Hypercube Designs for Continuous Factors
--	-----------	---

## Description

Generate the maximum projection (MaxPro) Latin hypercube design for continuous factors based on a simulated annealing algorithm. If nominal, discrete numeric, or ordinal factors exist, please see the function MaxProQQ.

## Usage

```
MaxProLHD(n, p, s=2, temp0=0, nstarts = 1, itermax = 400, total_iter = 1e+06)
```

## Arguments

n	The number of runs (design points)
р	The number of input factors (variables)
S	Optional, default is "2". The parameter in defining the s-norm distance (2 corresponds to Euclidean distance)
temp0	Optional, The initial temperature in the simulated annealing algorithm. Change this value if you want to start with a higher or lower temperature
nstarts	Optional, default is "1". The number of random starts
itermax	Optional, default is "400". The maximum number of non-improving searches allowed under each temperature. Lower this parameter if you want the algorithm to converge faster
total_iter	Optional, default is "1e+06". The maximum total number of iterations. Lower this number if the design is prohibitively large and you want to terminate the algorithm prematurely to report the best design found so far

#### **Details**

This function utilizes a version of the simulated annealing algorithm to efficiently generate the optimal Latin hypercube designs for continuous factors based on the MaxPro criterion. Parameters in the algorithm may need to be properly tuned to achieve global convergence. Please refer to Joseph, Gul and Ba (2015) for details.

#### Value

The value returned from the function is a list containing the following components:

Design	Design matrix
temp0	Initial temperature
measure	The MaxPro criterion measure
time_rec	Time to complete the search
ntotal	The total number of iterations

8 MaxProMeasure

#### Author(s)

Shan Ba <shanbatr@gmail.com> and V. Roshan Joseph <roshan@isye.gatech.edu>

#### References

Joseph, V. R., Gul, E., and Ba, S. (2015) "Maximum Projection Designs for Computer Experiments," *Biometrika*, 102, 371-380.

#### See Also

```
MaxProRunOrder, MaxProAugment, MaxProQQ
```

#### **Examples**

```
obj<-MaxProLHD(n = 10, p = 4)
obj$Design</pre>
```

MaxProMeasure

Maximum Projection Criterion Measure

## **Description**

Calculate the maximum projection (MaxPro) criterion measure for a given design.

#### Usage

```
MaxProMeasure(Design, p_nom=0)
```

## **Arguments**

Design The design matrix where each row is an experimental run and each column is a

factor. The rightmost p\_nom columns correspond to the p\_nom nominal factors, and the columns on the left are for continuous factors and discrete numeric factors. The ordinal factors, if any, should be pre-converted into discrete numeric factors through the scoring method (see, e.g., Wu and Hamada 2009, Section 14.10). All columns of the continuous and discrete numeric factors should be

standardized into the unit range of [0,1].

p\_nom Optional, default is "0". The number of nominal factors

#### **Details**

This function computes the MaxPro criterion measure for a given design. Please refer to Joseph, Gul and Ba (2015) and Joseph, Gul and Ba (2018) for details.

MaxProQQ 9

#### Value

The value returned from the function is the MaxPro criterion measure

#### Author(s)

Shan Ba <shanbatr@gmail.com> and V. Roshan Joseph <roshan@isye.gatech.edu>

#### References

Joseph, V. R., Gul, E., and Ba, S. (2015) "Maximum Projection Designs for Computer Experiments," *Biometrika*, 102, 371-380.

Joseph, V. R., Gul, E., and Ba, S. (2018) "Designing Computer Experiments with Multiple Types of Factors: The MaxPro Approach," *Journal of Quality Technology*, to appear.

Wu, C. F. J., and Hamada, M. (2009), *Experiments: Planning, Analysis, and Parameter Design Optimization*, 2nd Edition, New York: Wiley.

#### See Also

MaxProLHD, MaxProQQ, MaxProAugment

#### **Examples**

D<-MaxProLHD(10,2)\$Design
MaxProMeasure(D,p\_nom=0)</pre>

MaxProQQ

Maximum Projection Designs with Quantitative and Qualitative Factors

#### **Description**

Generate the maximum projection (MaxPro) design with quantitative and qualitative (QQ) factors. The quantitative factors can be continuous factors and/or discrete numeric factors, and the qualitative factors can be nominal factors and/or ordinal factors. If all factors are continuous, please use MaxProLHD directly.

To use this function, first convert all the ordinal factors into discrete numeric factors through the scoring method (see, e.g., Wu and Hamada 2009, Section 14.10). That is, if the ordinal factor has levels, "poor", "fair" and "good", then depending on the nature of the classification, the experimenter can choose some discrete numeric levels such as (1,2,3) or (1,4,5) to represent the three ordinal levels. Also, all columns of the continuous and discrete numeric factors should be standardized into the unit range of [0,1]

The users need to provide their desirable sub-design matrix for the nominal factors as part of the initial design input to this function. This function only optimizes the sub-design matrix of the continuous and discrete numeric factors as well as their row orders in joining with the pre-determined sub-design matrix of the nominal factors.

10 MaxProQQ

#### Usage

MaxProQQ(InitialDesign, p\_nom=0, temp0=0, nstarts=1, itermax=400, total\_iter=1e+06)

#### **Arguments**

InitialDesign The initial design matrix where each row is an experimental run and each col-

> umn is a factor. The rightmost p\_nom columns correspond to the p\_nom nominal factors, and the columns on the left are for continuous factors and discrete numeric factors (including ordinal factors). It is recommended to use a random Latin hypercube design as the initial design for continuous factors, and all columns of the continuous and discrete numeric factors should be standardized into the unit range of [0,1]. This function only optimizes the element permutations within the columns for continuous and discrete numeric factors. Elements in the last p\_nom columns are pre-determined by the user and fixed in this func-

tion.

Optional, default is "0". The number of nominal factors p\_nom

temp0 Optional, The initial temperature in the simulated annealing algorithm. Change

this value if you want to start with a higher or lower temperature

Optional, default is "1". The number of random starts nstarts

Optional, default is "400". The maximum number of non-improving searches itermax

allowed under each temperature. Lower this parameter if you want the algorithm

to converge faster

total\_iter Optional, default is "1e+06". The maximum total number of iterations. Lower

this number if the design is prohibitively large and you want to terminate the

algorithm prematurely to report the best design found so far

## **Details**

This function utilizes a version of the simulated annealing algorithm to efficiently generate the optimal design for continuous, nominal, discrete numeric and ordinal types of factors, where the design columns for nominal factors are pre-determined by the users and all the other columns are optimized based on the MaxProQQ criterion for the combined design. Parameters in the algorithm may need to be properly tuned to achieve global convergence. Please refer to Joseph, Gul and Ba (2018) for details.

### Value

temp0

The value returned from the function is a list containing the following components:

Design matrix Design Initial temperature

The MaxProQQ criterion measure measure

Time to complete the search time\_rec The total number of iterations ntotal

MaxProRunOrder 11

#### Author(s)

Shan Ba <shanbatr@gmail.com> and V. Roshan Joseph <roshan@isye.gatech.edu>

#### References

Joseph, V. R., Gul, E., and Ba, S. (2015) "Maximum Projection Designs for Computer Experiments," *Biometrika*, 102, 371-380.

Joseph, V. R., Gul, E., and Ba, S. (2018) "Designing Computer Experiments with Multiple Types of Factors: The MaxPro Approach," *Journal of Quality Technology*.

Wu, C. F. J., and Hamada, M. (2009), *Experiments: Planning, Analysis, and Parameter Design Optimization*, 2nd Edition, New York: Wiley.

#### See Also

MaxProRunOrder, MaxProAugment, MaxProLHD

## **Examples**

```
#18-run design
#3 continuous factors, 1 discrete numeric factor (6 levels), 2 nominal factors (3 levels)
#Generate a random Latin hypercube design (each factor standardized into [0,1])
#as the initial design for continuous factors
rand_design_part1=apply(matrix(rep(seq(from=0,to=1,length=18),3),ncol=3),2,sample)
#Generate a random initial design (standardized into [0,1]) for discrete numeric factors
rand_design_part2=sample(rep(seq(from=0,to=1,length=6),each=3))
#Construct an optimal design for the two nominal factors
OA_matrix=cbind(rep(1:3,each=6),rep(1:3,6))
#Initial design matrix
InitialDesign=cbind(rand_design_part1,rand_design_part2,OA_matrix)
#Optimize the design based on MaxProQQ criterion
obj=MaxProQQ(InitialDesign, p_nom=2)
obj$Design
```

MaxProRunOrder

Find the Optimal Sequential Order to Run a Given Experimental Design

12 MaxProRunOrder

#### **Description**

Given a computer experimental design matrix, this function searches for an optimal run (row) order based on the maximum projection (MaxPro) criterion. This optimal order enables the given design to be run in a sequential manner: when terminated at any step, the previous design points form a nearly optimal subset based on the MaxPro criterion.

## Usage

MaxProRunOrder(Design,p\_nom=0,initial\_row=1)

#### **Arguments**

Design The design matrix, where each row is an experimental run and each column is a

factor. The rightmost p\_nom columns correspond to the p\_nom nominal factors, and the columns on the left are for continuous factors and discrete numeric factors. The ordinal factors, if any, should be pre-converted into discrete numeric factors through the scoring method (see, e.g., Wu and Hamada 2009, Section 14.10). All columns of the continuous and discrete numeric factors should be

standardized into the unit range of [0,1].

p\_nom Optional, default is 0. The number of nominal factors

initial\_row Optional, default is 1. The vector specifying the row number of each design

point in the given design matrix that should be run at first or have already been

run.

#### Details

This function utilizes a greedy search algorithm to find the optimal row order to run the given experimental design based on the MaxPro criterion.

## Value

The value returned from the function is a list containing the following components:

Design The design matrix in optimal run (row) order. The run sequence ID is added as

the first column

measure The MaxPro criterion measure of the given design

time\_rec Time to complete the search

#### Author(s)

Shan Ba <shanbatr@gmail.com> and V. Roshan Joseph <roshan@isye.gatech.edu>

#### References

Joseph, V. R., Gul, E., and Ba, S. (2015) "Maximum Projection Designs for Computer Experiments," *Biometrika*, 102, 371-380.

Joseph, V. R. (2016) "Rejoinder," Quality Engineering, 28, 42-44.

MaxProRunOrder 13

Joseph, V. R., Gul, E., and Ba, S. (2018) "Designing Computer Experiments with Multiple Types of Factors: The MaxPro Approach," *Journal of Quality Technology*, to appear.

Wu, C. F. J., and Hamada, M. (2009), *Experiments: Planning, Analysis, and Parameter Design Optimization*, 2nd Edition, New York: Wiley.

#### See Also

MaxProLHD, MaxProQQ, MaxProAugment

## **Examples**

```
D0=MaxProLHD(25,2)$Design

#Assume the first two rows of the design have already been executed 
#Find the optimal run orders

D=MaxProRunOrder(D0,p_nom=0,initial_row=c(1,2))$Design 
plot(D[,2],D[,3],xlim=c(0,1),ylim=c(0,1),type="n", 
xlab=expression(x[1]),ylab=expression(x[2]),cex.lab=1.5) 
text(D[,2],D[,3],labels=D[,1],col='red')
```

## **Index**

```
* Computer Experiments
    CandPoints, 3
    MaxPro, 4
    MaxProAugment, 5
    MaxProLHD, 7
    MaxProMeasure, 8
    MaxProQQ, 9
    MaxProRunOrder, 11
* Design of Experiments
    CandPoints, 3
    MaxPro, 4
    MaxProAugment, 5
    MaxProLHD, 7
    MaxProMeasure, 8
    MaxProQQ, 9
    MaxProRunOrder, 11
* package
    MaxPro-package, 2
CandPoints, 3, 5, 6
MaxPro, 2, 4
MaxPro-package, 2
MaxProAugment, 2-4, 5, 8, 9, 11, 13
MaxProLHD, 2, 4, 6, 7, 9, 11, 13
MaxProMeasure, 2, 8
MaxProQQ, 2, 6-9, 9, 13
MaxProRunOrder, 2, 4, 8, 11, 11
```