

# Package ‘NTLKwIEx’

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**Type** Package

**Title** Computation of NTLKwIEx Distribution Properties

**Version** 0.1.0

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**Description** Implements statistical tools for analyzing, simulating, and computing properties of the New Topp-Leone Kumaraswamy Inverse Exponential (NTLKwIEx) distribution. See Atchadé M, Otodji T, and Djibril A (2024) <doi:10.1063/5.0179458> and Atchadé M, Otodji T, Djibril A, and N'bouké M (2023) <doi:10.1515/phys-2023-0151> for details.

**Depends** R (>= 3.6.0), stats, dplyr, ggplot2

**License** GPL-2

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 7.2.3

**VignetteBuilder** knitr

**Suggests** knitr, rmarkdown, testthat (>= 3.0.0)

**Language** fr

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**NeedsCompilation** no

**Repository** CRAN

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|-----------------------|---------------------------------------|
| ConductorFailureTimes | <i>Dataset: ConductorFailureTimes</i> |
|-----------------------|---------------------------------------|

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**Description**

This dataset contains failure times measured in hours from an accelerated life test with 59 conductors.

**Usage**

data(ConductorFailureTimes)

**Format**

A numeric vector of failure times.

**Details**

This dataset contains failure times (measured in hours) obtained from an accelerated life test involving 59 conductors. The data are presented as a numeric vector.

**References**

Nasiri, B., et al. (2010). "Bayesian analysis of the accelerated life model with Type-II censoring." Journal of Statistical Planning and Inference, 140(6), 1565-1572.

Schafft, H. A., et al. (1987). "Reproducibility of the accelerated test for electric cable insulation." IEEE Transactions on Electrical Insulation, 22(5), 739-746.

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|            |                                                                            |
|------------|----------------------------------------------------------------------------|
| C_NTLKwIEx | <i>Cumulative Distribution Function (CDF) of the NTLKwIEx distribution</i> |
|------------|----------------------------------------------------------------------------|

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**Description**

This function calculates the Cumulative density function (CDF) of the NTLKwIEx distribution.

**Usage**

C\_NTLKwIEx(x, teta, alpha, a, b, m)

**Arguments**

|       |                                                                                                        |
|-------|--------------------------------------------------------------------------------------------------------|
| x     | Value up to which to calculate the CDF.                                                                |
| teta  | Parameter teta of the distribution representing the distribution of the inverse exponential component. |
| alpha | Parameter alpha of the distribution representing the distribution of the new proposal component.       |
| a     | Parameter a of the distribution representing the distribution of the Kumaraswamy component.            |
| b     | Parameter b of the distribution representing the distribution of the Kumaraswamy component.            |
| m     | Parameter m of the distribution representing the distribution of the Topp Leone component.             |

**Details**

It takes parameters x, teta, alpha, a, b, and m, and returns the CDF value at x based on these parameters. The formula used for the calculation is provided in the documentation header. The Cumulative Distribution Function (CDF) of the NTLKwIEx distribution is defined as:

$$F(x; a, b, m, \alpha, \theta) = \left[ 1 - \left( 1 - K(x, \xi)^{a\alpha^{K(x, \xi)}} \right)^{2b} \right]^m$$

where  $\alpha, a, b, m, \theta > 0$ .

**Value**

Value of the CDF for the NTLKwIEx distribution evaluated at x

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E\_NTLKwIEx

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*Estimate parameters with constraints*


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**Description**

This function estimates the parameters of the NTLKwIEx distribution while adhering to parameter constraints. It employs the maximum likelihood estimation method and returns estimated values for each parameter based on a given dataset and the specified constraints.

**Usage**

```
E_NTLKwIEx(data)
```

**Arguments**

|      |                                |
|------|--------------------------------|
| data | Numeric vector of data values. |
|------|--------------------------------|

**Value**

Numeric vector of estimated parameters.

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|                |                                                                                                            |
|----------------|------------------------------------------------------------------------------------------------------------|
| Plot_CNTLKwIEx | <i>Graphical representation of the Cumulative Distribution Function (CDF) of the NTLKwIEx distribution</i> |
|----------------|------------------------------------------------------------------------------------------------------------|

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### Description

This function generates a plot of the Cumulative Distribution Function (CDF) of the NTLKwIEx distribution over a specified range of x values.

### Usage

```
Plot_CNTLKwIEx(teta, alpha, a, b, m, min_x, max_x)
```

### Arguments

|       |                                     |
|-------|-------------------------------------|
| teta  | Parameter teta of the distribution  |
| alpha | Parameter alpha of the distribution |
| a     | Parameter a of the distribution     |
| b     | Parameter b of the distribution     |
| m     | Parameter m of the distribution     |
| min_x | Minimum value of x for the plot     |
| max_x | Maximum value of x for the plot     |

### Value

A plot of the CDF of the NTLKwIEx distribution

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|                |                                                                                                        |
|----------------|--------------------------------------------------------------------------------------------------------|
| Plot_PNTLKwIEx | <i>Graphical representation of the probability density function (PDF) of the NTLKwIEx distribution</i> |
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### Description

This function generates a graph of the probability density function (PDF) of the NTLKwIEx distribution over a specified range of x values.

### Usage

```
Plot_PNTLKwIEx(teta, alpha, a, b, m, min_x, max_x)
```

**Arguments**

|       |                                     |
|-------|-------------------------------------|
| teta  | Parameter teta of the distribution  |
| alpha | Parameter alpha of the distribution |
| a     | Parameter a of the distribution     |
| b     | Parameter b of the distribution     |
| m     | Parameter m of the distribution     |
| min_x | Minimum value of x for the graph    |
| max_x | Maximum value of x for the graph    |

**Value**

A graph of the PDF of the NTLKwIEx distribution

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P\_NTLKwIEx

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*Probability Density Function (PDF) of the NTLKwIEx distribution*


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**Description**

The Probability Density Function (PDF) of the NTLKwIEx distribution is defined as:

**Usage**

P\_NTLKwIEx(x, teta, alpha, a, b, m)

**Arguments**

|       |                                     |
|-------|-------------------------------------|
| x     | Value to evaluate the PDF at        |
| teta  | Parameter teta of the distribution  |
| alpha | Parameter alpha of the distribution |
| a     | Parameter a of the distribution     |
| b     | Parameter b of the distribution     |
| m     | Parameter m of the distribution     |

**Details**

$$f(x, \theta, \alpha, a, b, m) = 2abm \frac{\theta}{x^2} \left( -\frac{\theta}{x} \log(\alpha) + \exp\left(\frac{\theta}{x}\right) \right) \exp\left\{ -\frac{\theta}{x} \left( 1 + a\alpha^{\exp\left(-\frac{\theta}{x}\right)} \right) \right\} \left\{ 1 - \exp\left( -a\frac{\theta}{x} \alpha^{\exp\left(-\frac{\theta}{x}\right)} \right) \right\}^{2b}$$

**Value**

Value of the PDF for the NTLKwIEx distribution evaluated at x

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|            |                                                    |
|------------|----------------------------------------------------|
| Q_NTLKwIEx | <i>Quantile Value of the NTLKwIEx distribution</i> |
|------------|----------------------------------------------------|

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**Description**

This function calculates the quantile value of the NTLKwIEx distribution for a given probability  $p$ .

**Usage**

```
Q_NTLKwIEx(p, teta, alpha, a, b, m)
```

**Arguments**

|       |                                                                                    |
|-------|------------------------------------------------------------------------------------|
| $p$   | Probability for which the quantile value is to be calculated ( $0 \leq p \leq 1$ ) |
| teta  | Parameter teta of the distribution                                                 |
| alpha | Parameter alpha of the distribution                                                |
| a     | Parameter a of the distribution                                                    |
| b     | Parameter b of the distribution                                                    |
| m     | Parameter m of the distribution                                                    |

**Value**

The quantile value corresponding to the probability  $p$  for the NTLKwIEx distribution

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|            |                                                       |
|------------|-------------------------------------------------------|
| R_NTLKwIEx | <i>Random Sampling from the NTLKwIEx distribution</i> |
|------------|-------------------------------------------------------|

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**Description**

This function generates random samples from the NTLKwIEx distribution based on the given parameters.

**Usage**

```
R_NTLKwIEx(n, teta, alpha, a, b, m)
```

**Arguments**

|       |                                      |
|-------|--------------------------------------|
| $n$   | Number of random samples to generate |
| teta  | Parameter teta of the distribution   |
| alpha | Parameter alpha of the distribution  |
| a     | Parameter a of the distribution      |
| b     | Parameter b of the distribution      |
| m     | Parameter m of the distribution      |

**Value**

A vector of n random samples from the NTLKwIEx distribution

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Sim\_NTLKwIEx

*Estimate parameters with constraints*

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**Description**

This function generates a histogram that depicts the distribution of the provided input data. Additionally, it estimates the parameters of a distribution that would correspond to the given data. By overlaying the estimated density function onto the histogram, Sim\_NTLKwIEx enables an immediate comparison between the empirical distribution and the estimated one. Sim\_NTLKwIEx proves to be a valuable tool for initial data exploration, streamlining trend identification, and understanding key features. Its usage comes recommended for tasks that require a swift exploratory analysis of data distributions.

**Usage**

```
Sim_NTLKwIEx(data)
```

**Arguments**

data                      Numeric vector of data values.

**Value**

Numeric vector of estimated parameters.

**Examples**

```
Sim_NTLKwIEx(c(38.181, 38.542, 38.928, 39.334, 35.8))
```

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## \* **datasets**

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