Package 'TSCI'

July 21, 2025

Title Tools for Causal Inference with Possibly Invalid Instrumental
Variables

Version 3.0.4

Description Two stage curvature identification with machine learning for causal
inference in settings when instrumental variable regression is not suitable
because of potentially invalid instrumental variables. Based on Guo and
Buehlmann (2022) ``Two Stage Curvature Identification with Machine Learning:
Causal Inference with Possibly Invalid Instrumental Variables''
<doi:10.48550/arXiv.2203.12808>. The vignette is available in Carl, Emmeneg-
ger, Bühlmann and Guo (2023)
``TSCI: two stage curvature identification for causal inference with
invalid instruments'' <doi:10.48550/arXiv.2304.00513>.

URL https://github.com/dlcarl/TSCI

License GPL (>= 3)

Encoding UTF-8

RoxygenNote 7.2.3

Depends R (>= 4.0.0)

Suggests fda, MASS, testthat (>= 3.0.0), withr

Config/testthat/edition 3

Imports xgboost, Rfast, stats, ranger, parallel, fastDummies

NeedsCompilation no

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Repository CRAN

Date/Publication 2023-10-09 18:50:02 UTC

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coef.tsci   *Extract Model Coefficients of TSCI Fits.*

Description

Extract Model Coefficients of TSCI Fits.

Usage

```
## S3 method for class 'tsci'
coef(object, parm = NULL, ...)
```

Arguments

object	an object of class 'tsci'.
parm	a specification for which treatment effect estimates should be returned. Either a vector of numbers or a vector of names or 'all'. If missing, the treatment effect estimate by violation space selection is returned. If 'all', the treatment effect estimates for all violation space candidates are returned.
...	arguments to be passed to or from other methods.

Value

Coefficients extracted form the model object object.

---

confint.tsci *Confidence Intervals of Treatment Effect Estimates for TSCI Fits.*

Description

Confidence Intervals of Treatment Effect Estimates for TSCI Fits.

Usage

```
## S3 method for class 'tsci'
confint(object, parm = NULL, level = 0.95, ...)
```

Arguments

object   an object of class 'tsci'.

parm   a specification of the parameters for which confidence intervals should be cal-
                culated. Either a vector of numbers or a vector of names or 'all'. If missing, the
                confidence interval of treatment effect estimate by violation space selection is
                returned. If 'all', the confidence intervals for all violation space candidates are
                returned.

level   the confidence level required.

...   additional argument(s) for methods.

Value

a matrix containing the confidence intervals.

---

create_interactions *Interactions as Violation Space Candidates*

Description

Interactions as Violation Space Candidates

Usage

```
create_interactions(Z, X = NULL)
```

Arguments

Z   observations of the instrumental variable(s). Either a numeric vector of length n
                or a numeric matrix with dimension n by s.

X   observations of baseline covariate(s) for which interactions with the instrumen-
                tal variable(s) should be part of the violation space candidates. Either a numeric
                vector of length n or a numeric matrix with dimension n by p or NULL (if only in-
                teractions between the instrumental variales itself should be part of the violation
                space candidates).

Value

A list. The first element contains the observations of the instrumental variable(s) Z. The second element contains all interactions between the instrumental variable(s) and the baseline covariate(s) X.

Examples

```
Z <- matrix(rnorm(100 * 3), nrow = 100, ncol = 3)
X <- matrix(rnorm(100 * 3), nrow = 100, ncol = 3)
vio_space <- create_interactions(Z = Z, X = X)
```

---

create_monomials   *Monomials as Violation Space Candidates*

Description

Monomials as Violation Space Candidates

Usage

```
create_monomials(Z, degree, type = c("monomials_main", "monomials_full"))
```

Arguments

Z	observations of the instrumental variable(s). Either a numeric vector of length n or a numeric matrix with dimension n by s.
degree	The degree up to which monomials should be created. Either a single positive integer or a vector of length s containing positive integers.
type	One out of monomials_main or monomials_full. monomials_main creates the monomials for the polynomials of each instrumental variable up to degree degree. monomials_full creates the monomials for the polynomials of a combination of all instrumental variables up to degree degree. Default is monomials_full.

Details

assuming there are 3 instrumental variables Z1, Z2, and Z3 and degree = c(d1, d2, d3) with d1 < d2 < d3, monomials_main creates the monomials of the polynomials $(Z1 + 1)^{d1}$, $(Z2 + 1)^{d2}$, $(Z3 + 1)^{d3}$ without the constants and monomials_full creates the monomials $(Z1 + Z2 + Z3)$, $(Z1 + Z2 + Z3)^2$, ..., $(Z1 + Z2 + Z3)^{d3}$ without the constants and excluding monomials that are products of $Z1^d$ or $Z2^d$ with $d > d1$ resp. $d > d2$. Thus type = monomials_main does not include interactions between the instrumental variables.

Value

A list. Each element is a matrix consisting of the monomials to be added to the next violation space candidate.

Examples

```
Z <- matrix(rnorm(100 * 3), nrow = 100, ncol = 3)
vio_space <- create_monomials(Z = Z, degree = 4, type = "monomials_full")
```

---

print.summary.tsci   *Print Content of summary.tsci Object.*

Description

Print Content of summary.tsci Object.

Usage

```
## S3 method for class 'summary.tsci'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

Arguments

x	an object of class 'summary.tsci'.
digits	number of significant digits to display.
...	arguments to be passed to or from other methods.

---

print.tsci   *Print Content of tsci Object.*

Description

Print Content of tsci Object.

Usage

```
## S3 method for class 'tsci'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

Arguments

x	an object of class 'tsci'.
digits	number of significant digits to display.
...	arguments to be passed to or from other methods.

summary.tsci   *Summarizing Two Stage Curvature Identification Fits*

Description

Summarizing Two Stage Curvature Identification Fits

Usage

```
## S3 method for class 'tsci'
summary(object, extended_output = FALSE, ...)
```

Arguments

object   an object of class 'tsci'.

extended_output

                  logical. If TRUE are more detailed summary is returned.

...   arguments to be passed to or from other methods.

Value

an object of class 'summary.tsci' containing the following elements:

coefficient a data frame with columns for the estimated treatment coefficient, its standard error, confidence interval and (two-sided) p-value.

invalidity a vector containing the number of times the instrumental variable(s) were considered valid, invalid or too weak to perform the test.

viospace_selection a data frame with columns for the number of times each of the violation space candidate was selected by comparison, the conservative method and as the largest violation space candidate for which the instrumental variable was considered to be strong enough.

treatment_model a data frame with information about the method used to fit the treatment model.

sample_size_A1 the number of observations in the subset used to fit the outcome model.

sample_size_A2 the number of observations in the subset used to train the parameters for fitting the treatment model.

n_splits the number of sample splits performed.

mult_split_method the method used to calculate the standard errors and p-values if n_splits is larger than 1.

alpha the significance level used.

iv_strength a data frame with columns containing the estimated instrumental variable strength and the estimated instrumental variable strength threshold for each violation space candidate. Will only be returned if extended_output is true.

coefficients_all a data frame with columns for the estimated treatment coefficients, its standard errors, confidence intervals and (two-sided) p-values for each violation space candidate.

---

tsci_boosting   *Two Stage Curvature Identification with Boosting*

Description

`tsci_boosting` implements Two Stage Curvature Identification (Guo and Buehlmann 2022) with boosting. Through a data-dependent way, it tests for the smallest sufficiently large violation space among a pre-specified sequence of nested violation space candidates. Point and uncertainty estimates of the treatment effect for all violation space candidates including the selected violation space will be returned amongst other relevant statistics.

Usage

```
tsci_boosting(
  Y,
  D,
  Z,
  X = NULL,
  W = X,
  vio_space,
  create_nested_sequence = TRUE,
  sel_method = c("comparison", "conservative"),
  split_prop = 2/3,
  nrounds = 50,
  eta = 0.3,
  max_depth = c(1:6),
  subsample = 1,
  colsample_bytree = 1,
  early_stopping = TRUE,
  nfolds = 5,
  self_predict = FALSE,
  sd_boot = TRUE,
  iv_threshold = 10,
  threshold_boot = TRUE,
  alpha = 0.05,
  intercept = TRUE,
  parallel = c("no", "multicore", "snow"),
  nsplits = 10,
  mult_split_method = c("FWER", "DML"),
  ncores = 1,
  cl = NULL,
  raw_output = NULL,
  B = 300
)
```

Arguments

Y	observations of the outcome variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If outcome variable is binary use dummy encoding.
D	observations of the treatment variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If treatment variable is binary use dummy encoding.
Z	observations of the instrumental variable(s). Either a vector of length n or a matrix with dimension n by s. If observations are not numeric dummy encoding will be applied.
X	observations of baseline covariate(s). Either a vector of length n or a matrix with dimension n by p or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
W	(transformed) observations of baseline covariate(s) used to fit the outcome model. Either a vector of length n or a matrix with dimension n by p_w or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
vio_space	list with vectors of length n and/or matrices with n rows as elements to specify the violation space candidates. If observations are not numeric dummy encoding will be applied. See Details for more information.
create_nested_sequence	
	logical. If TRUE, the violation space candidates (in form of matrices) are defined sequentially starting with an empty violation matrix and subsequently adding the next element of vio_space to the current violation matrix. If FALSE, the violation space candidates (in form of matrices) are defined as the empty space and the elements of vio_space. See Details for more information.
sel_method	The selection method used to estimate the treatment effect. Either "comparison" or "conservative". See Details.
split_prop	proportion of observations used to fit the outcome model. Has to be a value in (0, 1).
nrounds	number of boosting iterations. Can either be a single integer value or a vector of integer values to try.
eta	learning rate of the boosting algorithm. Can either be a single numeric value or a vector of numeric values to try.
max_depth	maximal tree depth. Can either be a single integer value or a vector of integer values to try.
subsample	subsample ratio of the training instance. Can either be a single numeric value or a vector of numeric values to try. Has to be a numeric value in (0, 1].
colsample_bytree	
	subsample ratio of columns when constructing each tree. Can either be a single numeric value or a vector of numeric values to try. Has to be a numeric value in (0, 1].
early_stopping	logical. If TRUE, early stopping will be applied to choose the optimal number of boosting iteration using the cross-validation mean squared error.

nfolds	a positive integer value specifying the number of folds used for cross-validation to choose best parameter combination.
self_predict	logical. If FALSE, it sets the diagonal of the hat matrix of each tree to zero to avoid self-prediction and rescales the off-diagonal elements accordingly.
sd_boot	logical. if TRUE, it determines the standard error using a bootstrap approach.
iv_threshold	a numeric value specifying the minimum of the threshold of IV strength test.
threshold_boot	logical. if TRUE, it determines the threshold of the IV strength using a bootstrap approach. If FALSE, it does not perform a bootstrap. See Details.
alpha	the significance level. Has to be a numeric value between 0 and 1.
intercept	logical. If TRUE, an intercept is included in the outcome model.
parallel	one out of "no", "multicore", or "snow" specifying the parallelization method used.
nsplits	number of times the data will be split. Has to be an integer larger or equal 1. See Details.
mult_split_method	method to calculate the standard errors, p-values and to construct the confidence intervals if multi-splitting is performed. Default is "DML" if nsplits == 1 and "FWER" otherwise. See Details.
ncores	the number of cores to use. Has to be an integer value larger or equal 1.
cl	either a parallel or snow cluster or NULL.
raw_output	logical. If TRUE, the coefficient and standard error estimates of each split will be returned. This is only needed for the use of the function confint if mult_split_method equals "FWER". Default is TRUE if mult_split_method is TRUE and FALSE otherwise.
B	number of bootstrap samples. Has to be a positive integer value. Bootstrap methods are used to calculate the IV strength threshold if threshold_boot is TRUE and for the violation space selection.

Details

The treatment and outcome models are assumed to be of the following forms:

$$D_i = f(Z_i, X_i) + \delta_i$$

$$Y_i = \beta \cdot D_i + h(Z_i, X_i) + \phi(X_i) + \epsilon_i$$

where $f(Z_i, X_i)$ is estimated using L2 boosting with regression trees as base learners, $h(Z_i X_i)$ is approximated using the violation space candidates and $\phi(X_i)$ is approximated by a linear combination of the columns in W. The errors are allowed to be heteroscedastic. To avoid overfitting bias the data is randomly split into two subsets $A1$ and $A2$ where the proportion of observations in the two sets is specified by split_prop. $A2$ is used to train the random forest and $A1$ is used to perform violation space selection and to estimate the treatment effect.

The package xgboost is used for boosting. If any of nrounds, eta, max_depth, subsample or colsample_bytree has more than one value, the best parameter combination is chosen by minimizing the cross-validation mean squared error.

The violation space candidates should be in a nested sequence as the violation space selection is performed by comparing the treatment estimate obtained by each violation space candidate with the estimates of all violation space candidates further down the list vio_space that provide enough IV strength. Only if no significant difference was found in all of those comparisons, the violation space candidate will be selected. If sel_method is 'comparison', the treatment effect estimate of this violation space candidate will be returned. If sel_method is 'conservative', the treatment effect estimate of the successive violation space candidate will be returned provided that the IV strength is large enough. The specification of suitable violation space candidates is a crucial step because a poor approximation of $g(Z_i, X_i)$ might not address the bias caused by the violation of the IV assumption sufficiently well. The function create_monomials can be used to create a predefined sequence of violation space candidates consisting of monomials. The function create_interactions can be used to create a predefined sequence of violation space candidates consisting of two-way interactions between the instrumens themselves and between the instruments and the instruments and baseline covariates.

W should be chosen to be flexible enough to approximate the functional form of ϕ well as otherwise the treatment estimator might be biased.

The instrumental variable(s) are considered strong enough for violation space candidate V_q if the estimated IV strength using this violation space candidate is larger than the obtained value of the threshold of the IV strength. The formula of the threshold of the IV strength has the form $\min\{\max\{2\cdot\mathrm{Trace}[\mathrm{M}(V_q)], \mathrm{iv\_threshold}\}+S(V_q), 40\}$ if threshold_boot is TRUE, and $\min\{\max\{2\cdot \mathrm{Trace}[\mathrm{M}(V_q)], \mathrm{iv\_threshold}\}, 40\}$ if threshold_boot is FALSE. The matrix $\mathrm{M}(V_q)$ depends on the hat matrix obtained from estimating $f(Z_i, X_i)$, the violation space candidate V_q and the variables to include in the outcome model W. $S(V_q)$ is obtained using a bootstrap and aims to adjust for the estimation error of the IV strength. Usually, the value of the threshold of the IV strength obtained using the bootstrap approach is larger. Thus, using threshold_boot equals TRUE leads to a more conservative IV strength test. For more information see subsection 3.3 in Guo and Buehlmann (2022).

nsplits specifies the number of data splits that should be performed. For each data split the output statistics such as the point estimates of the treatment effect are calculated. Those statistics will then be aggregated over the different data splits. It is recommended to perform multiple data splits as data splitting introduces additional randomness. By aggregating the results of multiple data splits, the effects of this randomness can be decreased. If nsplits is larger than 1, point estimates are aggregated by medians. Standard errors, p-values and confidence intervals are obtained by the method specified by the parameter mult_split_method. 'DML' uses the approach by Chernozhukov et al. (2018). 'FWER' uses the approach by Meinshausen et al. (2009) and controls for the family-wise error rate. 'FWER' does not provide standard errors. For large sample sizes, a large values for nsplits can lead to a high running time as for each split a new hat matrix must be calculated.

There are three possibilities to set the argument parallel, namely "no" for serial evaluation (default), "multicore" for parallel evaluation using forking, and "snow" for parallel evaluation using a parallel socket cluster. It is recommended to select RNGkind ("L'Ecuyer-CMRG") and to set a seed to ensure that the parallel computing of the package TSCI is reproducible. This ensures that each processor receives a different substream of the pseudo random number generator stream. Thus, the results are reproducible if the arguments (including ncores) remain unchanged. There is an op-

tional argument `cl` to specify a custom cluster if `parallel = "snow"`.

See also Carl et al. (2023) for more details.

Value

A list containing the following elements:

`Coef_all` a series of point estimates of the treatment effect obtained by the different violation space candidates.

`sd_all` standard errors of the estimates of the treatmnet effect obtained by the different violation space candidates.

`pval_all` p-values of the treatment effect estimates obtained by the different violation space candidates.

`CI_all` confidence intervals for the treatment effect obtained by the different violation space candidates.

`Coef_sel` the point estimator of the treatment effect obtained by the selected violation space candidate(s).

`sd_sel` the standard error of Coef_sel.

`pval_sel` p-value of the treatment effect estimate obtained by the selected violation space candidate(s).

`CI_sel` confidence interval for the treatment effect obtained by the selected violation space candidate(s).

`iv_str` IV strength using the different violation space candidates.

`iv_thol` the threshold for the IV strength using the different violation space candidates.

`Qmax` the frequency each violation space candidate was the largest violation space candidate for which the IV strength was considered large enough determined by the IV strength test over the multiple data splits. If 0, the IV Strength test failed for the first violation space candidate. Otherwise, violation space selection was performed.

`q_comp` the frequency each violation space candidate was selected by the comparison method over the multiple data splits.

`q_cons` the frequency each violation space candidate was selected by the conservative method over the multiple data splits.

`invalidity` the frequency the instrumental variable(s) were considered valid, invalid or too weak to test for violations. The instrumental variables are considered too weak to test for violations if the IV strength is already too weak using the first violation space candidate (besides the empty violation space). Testing for violations is always performed by using the comparison method.

`mse` the out-of-sample mean squared error of the fitted treatment model.

`FirstStage_model` the method used to fit the treatment model.

`n_A1` number of observations in A1.

`n_A2` number of observations in A2.

`nsplits` number of data splits performed.

`mult_split_method` the method used to calculate the standard errors and p-values.

`alpha` the significance level used.

References

- Zijian Guo, and Peter Buehlmann. Two Stage Curvature Identification with Machine Learning: Causal Inference with Possibly Invalid Instrumental Variables. *arXiv:2203.12808*, 2022

- Nicolai Meinshausen, Lukas Meier, and Peter Buehlmann. P-values for high-dimensional regression. *Journal of the American Statistical Association*, 104(488):1671-1681, 2009. 16, 18

- Victor Chernozhukov, Denis Chetverikov, Mert Demirer, Esther Duflo, Christian Hansen, Whitney Newey, and James Robins. Double/debiased machine learning for treatment and structural parameters: Double/debiased machine learning. *The Econometrics Journal*, 21(1), 2018. 4, 16, 18

- David Carl, Corinne Emmenegger, Peter Buehlmann, and Zijian Guo. TSCI: two stage curvature identification for causal inference with invalid instruments. *arXiv:2304.00513*, 2023

See Also

`tsci_forest` for TSCI with random forest.

`tsci_poly` for TSCI with polynomial basis expansion.

`tsci_secondstage` for TSCI with user provided hat matrix.

Examples

```
### a small example without baseline covariates
if (require("MASS")) {
  # sample size
  n <- 100
  # the IV strength
  a <- 1
  # the violation strength
  tau <- 1
  # true effect
  beta <- 1
  # treatment model
  f <- function(x) {1 + a * (x + x^2)}
  # outcome model
  g <- function(x) {1 + tau * x}

  # generate data
  mu_error <- rep(0, 2)
  Cov_error <- matrix(c(1, 0.5, 0.5, 1), 2, 2)
  Error <- MASS::mvrnorm(n, mu_error, Cov_error)
  # instrumental variable
  Z <- rnorm(n)
  # treatment variable
  D <- f(Z) + Error[, 1]
  # outcome variable
  Y <- beta * D + g(Z) + Error[, 2]
```

```
     # Two Stage L2 Boosting
     # create violation space candidates
     vio_space <- create_monomials(Z, 2, "monomials_main")
     # perform two stage curvature identification
     output_BO <- tsci_boosting(Y, D, Z, vio_space = vio_space, nsplits = 1,
                                max_depth = 2, nrounds = 10, B = 100)
     summary(output_BO)
 }
```

---

tsci_forest	*Two Stage Curvature Identification with Random Forests*

Description

`tsci_forest` implements Two Stage Curvature Identification (Guo and Buehlmann 2022) with random forests. Through a data-dependent way, it tests for the smallest sufficiently large violation space among a pre-specified sequence of nested violation space candidates. Point and uncertainty estimates of the treatment effect for all violation space candidates including the selected violation space will be returned amongst other relevant statistics.

Usage

```
tsci_forest(
  Y,
  D,
  Z,
  X = NULL,
  W = X,
  vio_space,
  create_nested_sequence = TRUE,
  sel_method = c("comparison", "conservative"),
  split_prop = 2/3,
  num_trees = 200,
  mtry = NULL,
  max_depth = 0,
  min_node_size = c(5, 10, 20),
  self_predict = FALSE,
  sd_boot = TRUE,
  iv_threshold = 10,
  threshold_boot = TRUE,
  alpha = 0.05,
  nsplits = 10,
  mult_split_method = c("FWER", "DML"),
  intercept = TRUE,
  parallel = c("no", "multicore", "snow"),
  ncores = 1,
  cl = NULL,
```

```
  raw_output = NULL,
  B = 300
)
```

Arguments

Y	observations of the outcome variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If outcome variable is binary use dummy encoding.
D	observations of the treatment variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If treatment variable is binary use dummy encoding.
Z	observations of the instrumental variable(s). Either a vector of length n or a matrix with dimension n by s. If observations are not numeric dummy encoding will be applied.
X	observations of baseline covariate(s). Either a vector of length n or a matrix with dimension n by p or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
W	(transformed) observations of baseline covariate(s) used to fit the outcome model. Either a vector of length n or a matrix with dimension n by p_w or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
vio_space	list with vectors of length n and/or matrices with n rows as elements to specify the violation space candidates. If observations are not numeric dummy encoding will be applied. See Details for more information.
create_nested_sequence	
	logical. If TRUE, the violation space candidates (in form of matrices) are defined sequentially starting with an empty violation matrix and subsequently adding the next element of vio_space to the current violation matrix. If FALSE, the violation space candidates (in form of matrices) are defined as the empty space and the elements of vio_space. See Details for more information.
sel_method	the selection method used to estimate the treatment effect. Either "comparison" or "conservative". See Details.
split_prop	proportion of observations used to fit the outcome model. Has to be a numeric value in (0, 1).
num_trees	number of trees in random forests. Can either be a single integer value or a vector of integer values to try.
mtry	number of covariates to possibly split at in each node of the tree of the random forest. Can either be a single integer value or a vector of integer values to try. Can also be a list of single argument function(s) returning an integer value, given the number of independent variables. The values have to be positive integers not larger than the number of independent variables in the treatment model. Default is to try all integer values between one-third of the independent variables and two-thirds of the independent variables.
max_depth	maximal tree depth in random forests. Can either be a single integer value or a vector of integer values to try. 0 correspond to unlimited depth.

min_node_size	minimal size of each leaf node in the random forest. Can either be a single integer value or a vector of integer values to try.
self_predict	logical. If FALSE, it sets the diagonal of the hat matrix of each tree to zero to avoid self-prediction and rescales the off-diagonal elements accordingly.
sd_boot	logical. if TRUE, it determines the standard error using a bootstrap approach.
iv_threshold	a numeric value specifying the minimum of the threshold of IV strength test.
threshold_boot	logical. If TRUE, it determines the threshold of the IV strength using a bootstrap approach. If FALSE, it does not perform a bootstrap. See Details.
alpha	the significance level. Has to be a numeric value between 0 and 1.
nsplits	number of times the data will be split. Has to be an integer larger or equal 1. See Details.
mult_split_method	
	method to calculate the standard errors, p-values and to construct the confidence intervals if multi-splitting is performed. Default is "DML" if nsplits == 1 and "FWER" otherwise. See Details.
intercept	logical. If TRUE, an intercept is included in the outcome model.
parallel	one out of "no", "multicore", or "snow" specifying the parallelization method used. See Details.
ncores	the number of cores to use. Has to be an integer value larger or equal 1.
cl	either a parallel or snow cluster or NULL.
raw_output	logical. If TRUE, the coefficient and standard error estimates of each split will be returned. This is only needed for the use of the function confint if mult_split_method equals "FWER". Default is TRUE if mult_split_method is TRUE and FALSE otherwise.
B	number of bootstrap samples. Has to be a positive integer value. Bootstrap methods are used to calculate the IV strength threshold if threshold_boot is TRUE and for the violation space selection. It is also used to calculate the standard error if sd_boot is TRUE.

Details

The treatment and outcome models are assumed to be of the following forms:

$$D_i = f(Z_i, X_i) + \delta_i$$

$$Y_i = \beta \cdot D_i + h(Z_i, X_i) + \phi(X_i) + \epsilon_i$$

where $f(Z_i, X_i)$ is estimated using a random forest, $h(Z_i X_i)$ is approximated using the violation space candidates and $\phi(X_i)$ is approximated by a linear combination of the columns in W. The errors are allowed to be heteroscedastic. To avoid overfitting bias the data is randomly split into two subsets $A1$ and $A2$ where the proportion of observations in the two sets is specified by split_prop. $A2$ is used to train the random forest and $A1$ is used to perform violation space selection and to estimate the treatment effect.

The package ranger is used to fit the random forest. If any of num_trees, max_depth or min_node_size has more than one value, the best parameter combination is chosen by minimizing the out-of-bag

mean squared error.

The violation space candidates should be in a nested sequence as the violation space selection is performed by comparing the treatment estimate obtained by each violation space candidate with the estimates of all violation space candidates further down the list vio_space that provide enough IV strength. Only if no significant difference was found in all of those comparisons, the violation space candidate will be selected. If sel_method is 'comparison', the treatment effect estimate of this violation space candidate will be returned. If sel_method is 'conservative', the treatment effect estimate of the successive violation space candidate will be returned provided that the IV strength is large enough. The specification of suitable violation space candidates is a crucial step because a poor approximation of $g(Z_i, X_i)$ might not address the bias caused by the violation of the IV assumption sufficiently well. The function create_monomials can be used to create a predefined sequence of violation space candidates consisting of monomials. The function create_interactions can be used to create a predefined sequence of violation space candidates consisting of two-way interactions between the instrumens themselves and between the instruments and the instruments and baseline covariates.

The instrumental variable(s) are considered strong enough for violation space candidate V_q if the estimated IV strength using this violation space candidate is larger than the obtained value of the threshold of the IV strength. The formula of the threshold of the IV strength has the form $\min\{\max\{2 \cdot \text{Trace}[\text{M}(V_q)], \text{iv\_threshold}\} + S(V_q), 40\}$ if threshold_boot is TRUE, and $\min\{\max\{2 \cdot \text{Trace}[\text{M}(V_q)], \text{iv\_threshold}\}, 40\}$ if threshold_boot is FALSE. The matrix $\text{M}(V_q)$ depends on the hat matrix obtained from estimating $f(Z_i, X_i)$, the violation space candidate V_q and the variables to include in the outcome model W. $S(V_q)$ is obtained using a bootstrap and aims to adjust for the estimation error of the IV strength. Usually, the value of the threshold of the IV strength obtained using the bootstrap approach is larger. Thus, using threshold_boot equals TRUE leads to a more conservative IV strength test. For more information see subsection 3.3 in Guo and Buehlmann (2022).

nsplits specifies the number of data splits that should be performed. For each data split the output statistics such as the point estimates of the treatment effect are calculated. Those statistics will then be aggregated over the different data splits. It is recommended to perform multiple data splits as data splitting introduces additional randomness. By aggregating the results of multiple data splits, the effects of this randomness can be decreased. If nsplits is larger than 1, point estimates are aggregated by medians. Standard errors, p-values and confidence intervals are obtained by the method specified by the parameter mult_split_method. 'DML' uses the approach by Chernozhukov et al. (2018). 'FWER' uses the approach by Meinshausen et al. (2009) and controls for the family-wise error rate. 'FWER' does not provide standard errors. For large sample sizes, a large values for nsplits can lead to a high running time as for each split a new hat matrix must be calculated.

There are three possibilities to set the argument parallel, namely "no" for serial evaluation (default), "multicore" for parallel evaluation using forking, and "snow" for parallel evaluation using a parallel socket cluster. It is recommended to select RNGkind ("L'Ecuyer-CMRG") and to set a seed to ensure that the parallel computing of the package TSCI is reproducible. This ensures that each processor receives a different substream of the pseudo random number generator stream. Thus, the results are reproducible if the arguments (including ncores) remain unchanged. There is an optional argument cl to specify a custom cluster if parallel = "snow".

Results obtained on different operating systems might differ even when the same seed is set. The reason for this lies in the way the random forest algorithm in ranger is implemented. Currently, we are not aware of a solution to ensure reproducibility across operating systems when using tsci_forest. However, tsci_boosting, tsci_poly and tsci_secondstage do not have this issue.

See also Carl et al. (2023) for more details.

Value

A list containing the following elements:

Coef_all a series of point estimates of the treatment effect obtained by the different violation space candidates.

sd_all standard errors of the estimates of the treatmnet effect obtained by the different violation space candidates.

pval_all p-values of the treatment effect estimates obtained by the different violation space candidates.

CI_all confidence intervals for the treatment effect obtained by the different violation space candidates.

Coef_sel the point estimator of the treatment effect obtained by the selected violation space candidate(s).

sd_sel the standard error of Coef_sel.

pval_sel p-value of the treatment effect estimate obtained by the selected violation space candidate(s).

CI_sel confidence interval for the treatment effect obtained by the selected violation space candidate(s).

iv_str IV strength using the different violation space candidates.

iv_thol the threshold for the IV strength using the different violation space candidates.

Qmax the frequency each violation space candidate was the largest violation space candidate for which the IV strength was considered large enough determined by the IV strength test over the multiple data splits. If 0, the IV Strength test failed for the first violation space candidate. Otherwise, violation space selection was performed.

q_comp the frequency each violation space candidate was selected by the comparison method over the multiple data splits.

q_cons the frequency each violation space candidate was selected by the conservative method over the multiple data splits.

invalidity the frequency the instrumental variable(s) were considered valid, invalid or too weak to test for violations. The instrumental variables are considered too weak to test for violations if the IV strength is already too weak using the first violation space candidate (besides the empty violation space). Testing for violations is always performed by using the comparison method.

mse the out-of-sample mean squared error of the fitted treatment model.

FirstStage_model the method used to fit the treatment model.

n_A1 number of observations in A1.

n_A2 number of observations in A2.

nsplits number of data splits performed.

mult_split_method the method used to calculate the standard errors and p-values.

alpha the significance level used.

References

- Zijian Guo, and Peter Buehlmann. Two Stage Curvature Identification with Machine Learning: Causal Inference with Possibly Invalid Instrumental Variables. *arXiv:2203.12808*, 2022

- Nicolai Meinshausen, Lukas Meier, and Peter Buehlmann. P-values for high-dimensional regression. *Journal of the American Statistical Association*, 104(488):1671-1681, 2009. 16, 18

- Victor Chernozhukov, Denis Chetverikov, Mert Demirer, Esther Duflo, Christian Hansen, Whitney Newey, and James Robins. Double/debiased machine learning for treatment and structural parameters: Double/debiased machine learning. *The Econometrics Journal*, 21(1), 2018. 4, 16, 18

- David Carl, Corinne Emmenegger, Peter Buehlmann, and Zijian Guo. TSCI: two stage curvature identification for causal inference with invalid instruments. *arXiv:2304.00513*, 2023

See Also

tsci_boosting for TSCI with boosting.

tsci_poly for TSCI with polynomial basis expansion.

tsci_secondstage for TSCI with user provided hat matrix.

Examples

```
### a small example without baseline covariates
if (require("MASS")) {
  # sample size
  n <- 100
  # the IV strength
  a <- 1
  # the violation strength
  tau <- 1
  # true effect
  beta <- 1
  # treatment model
  f <- function(x) {1 + a * (x + x^2)}
  # outcome model
  g <- function(x) {1 + tau * x}

  # generate data
  mu_error <- rep(0, 2)
  Cov_error <- matrix(c(1, 0.5, 0.5, 1), 2, 2)
```

```
      Error <- MASS::mvrnorm(n, mu_error, Cov_error)
      # instrumental variable
      Z <- rnorm(n)
      # treatment variable
      D <- f(Z) + Error[, 1]
      # outcome variable
      Y <- beta * D + g(Z) + Error[, 2]

      # Two Stage Random Forest
      # create violation space candidates
      vio_space <- create_monomials(Z, 2, "monomials_main")
      # perform two stage curvature identification
      output_RF <- tsci_forest(Y, D, Z, vio_space = vio_space, nsplits = 1,
                               num_trees = 50, B = 100)
      summary(output_RF)
   }
```

---

tsci_poly   *Two Stage Curvature Identification with Polynomial Basis Expansion*

Description

`tsci_poly` implements Two Stage Curvature Identification (Guo and Buehlmann 2022) with a basis expansion by monomials. Through a data-dependent way it tests for the smallest sufficiently large violation space among a pre-specified sequence of nested violation space candidates. Point and uncertainty estimates of the treatment effect for all violation space candidates including the selected violation space will be returned amongst other relevant statistics.

Usage

```
tsci_poly(
  Y,
  D,
  Z,
  X = NULL,
  W = X,
  vio_space = NULL,
  create_nested_sequence = TRUE,
  sel_method = c("comparison", "conservative"),
  min_order = 1,
  max_order = 10,
  exact_order = NULL,
  order_selection_method = c("grid search", "backfitting"),
  max_iter = 100,
  conv_tol = 10^-6,
  gcv = FALSE,
  nfolds = 5,
  sd_boot = TRUE,
```

```
    iv_threshold = 10,
    threshold_boot = TRUE,
    alpha = 0.05,
    intercept = TRUE,
    B = 300
)
```

Arguments

Y	observations of the outcome variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If outcome variable is binary use dummy encoding.
D	observations of the treatment variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If treatment variable is binary use dummy encoding.
Z	observations of the instrumental variable(s). Either a vector of length n or a matrix with dimension n by s. If observations are not numeric dummy encoding will be applied.
X	observations of baseline covariate(s). Either a vector of length n or a matrix with dimension n by p or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
W	(transformed) observations of baseline covariate(s) used to fit the outcome model. Either a vector of length n or a matrix with dimension n by p_w or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
vio_space	either NULL or a list with numeric vectors of length n and/or numeric matrices with n rows as elements to specify the violation space candidates. If observations are not numeric dummy encoding will be applied. See Details for more information. If NULL, then the violation space candidates are chosen to be a nested sequence of monomials with degree depending on the orders of the polynomials used to fit the treatment model.
create_nested_sequence	
	logical. If TRUE, the violation space candidates (in form of matrices) are defined sequentially starting with an empty violation matrix and subsequently adding the next element of vio_space to the current violation matrix. If FALSE, the violation space candidates (in form of matrices) are defined as the empty space and the elements of vio_space. See Details for more information.
sel_method	The selection method used to estimate the treatment effect. Either "comparison" or "conservative". See Details.
min_order	either a single integer value or a vector of integer values of length s specifying the smallest order of polynomials to use in the selection of the treatment model. If a single integer value is provided, the polynomials of all instrumental variables use this value.
max_order	either a single integer value or a vector of integer values of length s specifying the largest order of polynomials to use in the selection of the treatment model. If a single integer value is provided, the polynomials of all instrumental variables use this value.

exact_order	either a single integer value or a vector of integer values of length s specifying the exact order of polynomials to use in the treatment model. If a single integer value is provided, the polynomials of all instrumental variables use this value.
order_selection_method	
	method used to select the best fitting order of polynomials for the treatment model. Must be either 'grid search' or 'backfitting'. 'grid search' can be very slow if the number of instruments is large.
max_iter	number of iterations used in the backfitting algorithm if order_selection_method is 'backfitting'. Has to be a positive integer value.
conv_tol	tolerance of convergence in the backfitting algorithm if order_selection_method is 'backfitting'.
gcv	logical. If TRUE, the generalized cross-validation mean squared error is used to determine the best fitting order of polynomials for the treatment model. If FALSE, k-fold cross-validation is used instead.
nfolds	number of folds used for the k-fold cross-validation if gcv is FALSE. Has to be a positive integer value.
sd_boot	logical. if TRUE, it determines the standard error using a bootstrap approach.
iv_threshold	a numeric value specifying the minimum of the threshold of IV strength test.
threshold_boot	logical. if TRUE, it determines the threshold of the IV strength using a bootstrap approach. If FALSE, it does not perform a bootstrap. See Details.
alpha	the significance level. Has to be a numeric value between 0 and 1.
intercept	logical. If TRUE, an intercept is included in the outcome model.
B	number of bootstrap samples. Has to be a positive integer value. Bootstrap methods are used to calculate the iv strength threshold if threshold_boot is TRUE and for the violation space selection.

Details

The treatment and outcome models are assumed to be of the following forms:

$$D_i = f(Z_i, X_i) + \delta_i$$

$$Y_i = \beta \cdot D_i + h(Z_i, X_i) + \phi(X_i) + \epsilon_i$$

where $f(Z_i, X_i)$ is estimated using a polynomial basis expansion of the instrumental variables and a linear combination of the baseline covariates, $h(Z_i X_i)$ is approximated using the violation space candidates and $\phi(X_i)$ is approximated by a linear combination of the columns in W. The errors are allowed to be heteroscedastic.

The violation space candidates should be in a nested sequence as the violation space selection is performed by comparing the treatment estimate obtained by each violation space candidate with the estimates of all violation space candidates further down the list vio_space that provide enough IV strength. Only if no significant difference was found in all of those comparisons, the violation space candidate will be selected. If sel_method is 'comparison', the treatment effect estimate of this violation space candidate will be returned. If sel_method is 'conservative', the treatment effect estimate of the successive violation space candidate will be returned provided that the IV strength

is large enough. If `vio_space` is `NULL` the violation space candidates are chosen to be a nested sequence of polynomials of the instrumental variables up to the degrees used to fit the treatment model. This guarantees that the possible spaces of the violation will be tested. If the functional form of the outcome model is not well-known it is advisable to use the default values for `W` and `vio_space`.

The instrumental variable(s) are considered strong enough for violation space candidate V_q if the estimated IV strength using this violation space candidate is larger than the obtained value of the threshold of the IV strength. The formula of the threshold of the IV strength has the form $\min\{\max\{2 \cdot \text{Trace}[\text{M}(V_q)], \text{iv\_threshold}\} + S(V_q), 40\}$ if `threshold_boot` is `TRUE`, and $\min\{\max\{2 \cdot \text{Trace}[\text{M}(V_q)], \text{iv\_threshold}\}, 40\}$ if `threshold_boot` is `FALSE`. The matrix $\text{M}(V_q)$ depends on the hat matrix obtained from estimating $f(Z_i, X_i)$, the violation space candidate V_q and the variables to include in the outcome model `W`. $S(V_q)$ is obtained using a bootstrap and aims to adjust for the estimation error of the IV strength. Usually, the value of the threshold of the IV strength obtained using the bootstrap approach is larger. Thus, using `threshold_boot` equals `TRUE` leads to a more conservative IV strength test. For more information see subsection 3.3 in Guo and Buehlmann (2022).

See also Carl et al. (2023) for more details.

Value

A list containing the following elements:

Coef_all a series of point estimates of the treatment effect obtained by the different violation space candidates.

sd_all standard errors of the estimates of the treatmnet effect obtained by the different violation space candidates.

pval_all p-values of the treatment effect estimates obtained by the different violation space candidates.

CI_all confidence intervals for the treatment effect obtained by the different violation space candidates.

Coef_sel the point estimator of the treatment effect obtained by the selected violation space candidate(s).

sd_sel the standard error of Coef_sel.

pval_sel p-value of the treatment effect estimate obtained by the selected violation space candidate(s).

CI_sel confidence interval for the treatment effect obtained by the selected violation space candidate(s).

iv_str IV strength using the different violation space candidates.

iv_thol the threshold for the IV strength using the different violation space candidates.

Qmax the violation space candidate that was the largest violation space candidate for which the IV strength was considered large enough determined by the IV strength test. If 0, the IV Strength test failed for the first violation space candidate. Otherwise, violation space selection was performed.

q_comp the violation space candidate that was selected by the comparison method over the multiple data splits.

q_cons the violation space candidate that was selected by the conservative method over the multiple data splits.

invalidity shows whether the instrumental variable(s) were considered valid, invalid or too weak to test for violations. The instrumental variables are considered too weak to test for violations if the IV strength is already too weak using the first violation space candidate (besides the empty violation space). Testing for violations is always performed by using the comparison method.

mse the out-of-sample mean squared error of the treatment model.

References

- Zijian Guo, and Peter Buehlmann. Two Stage Curvature Identification with Machine Learning: Causal Inference with Possibly Invalid Instrumental Variables. *arXiv:2203.12808*, 2022
- David Carl, Corinne Emmenegger, Peter Buehlmann, and Zijian Guo. TSCI: two stage curvature identification for causal inference with invalid instruments. *arXiv:2304.00513*, 2023

See Also

[tsci_forest](#) for TSCI with random forest.

[tsci_boosting](#) for TSCI with boosting.

[tsci_secondstage](#) for TSCI with user provided hat matrix.

Examples

```
### a small example without baseline covariates
if (require("MASS")) {
  # sample size
  n <- 100
  # the IV strength
  a <- 1
  # the violation strength
  tau <- 1
  # true effect
  beta <- 1
  # treatment model
  f <- function(x) {1 + a * (x + x^2)}
  # outcome model
  g <- function(x) {1 + tau * x}

  # generate data
  mu_error <- rep(0, 2)
  Cov_error <- matrix(c(1, 0.5, 0.5, 1), 2, 2)
  Error <- MASS::mvrnorm(n, mu_error, Cov_error)
  # instrumental variable
```

```
  Z <- rnorm(n)
  # treatment variable
  D <- f(Z) + Error[, 1]
  # outcome variable
  Y <- beta * D + g(Z) + Error[, 2]

  # Two Stage Polynomials
  output_PO <- tsci_poly(Y, D, Z, max_order = 3, max_iter = 20, B = 100)
  summary(output_PO)
}
```

---

tsci_secondstage	*Two Stage Curvature Identification with User Provided Hat Matrix*

Description

`tsci_secondstage` implements Two Stage Curvature Identification (Guo and Buehlmann 2022) for a user-provided hat matrix. Through a data-dependent way it tests for the smallest sufficiently large violation space among a pre-specified sequence of nested violation space candidates. Point and uncertainty estimates of the treatment effect for all violation space candidates including the selected violation space will be returned amongst other relevant statistics.

Usage

```
tsci_secondstage(
  Y,
  D,
  Z,
  W = NULL,
  vio_space,
  create_nested_sequence = TRUE,
  weight,
  A1_ind = NULL,
  sel_method = c("comparison", "conservative"),
  sd_boot = TRUE,
  iv_threshold = 10,
  threshold_boot = TRUE,
  alpha = 0.05,
  intercept = TRUE,
  B = 300
)
```

Arguments

Y   observations of the outcome variable. Either a numeric vector of length n or a
                     numeric matrix with dimension n by 1. If outcome variable is binary use dummy
                     encoding.

D   observations of the treatment variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If treatment variable is binary use dummy encoding.

Z   observations of the instrumental variable(s). Either a vector of length n or a matrix with dimension n by s. If observations are not numeric dummy encoding will be applied.

W   (transformed) observations of baseline covariate(s) used to fit the outcome model. Either a vector of length n or a matrix with dimension n by p_w or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.

vio_space   list with vectors of length n and/or matrices with n rows as elements to specify the violation space candidates. If observations are not numeric dummy encoding will be applied. See Details for more information.

create_nested_sequence
                     logical. If TRUE, the violation space candidates (in form of matrices) are defined sequentially starting with an empty violation matrix and subsequently adding the next element of vio_space to the current violation matrix. If FALSE, the violation space candidates (in form of matrices) are defined as the empty space and the elements of vio_space. See Details for more information.

weight   the hat matrix of the treatment model.

A1_ind   indices of the observations that wil be used to fit the outcome model. Must be of same length as the number of rows and columns of weight. If NULL, all observations will be used.

sel_method   The selection method used to estimate the treatment effect. Either "comparison" or "conservative". See Details.

sd_boot   logical. if TRUE, it determines the standard error using a bootstrap approach.

iv_threshold   a numeric value specifying the minimum of the threshold of IV strength test.

threshold_boot   logical. if TRUE, it determines the threshold of the IV strength using a bootstrap approach. If FALSE, it does not perform a bootstrap. See Details.

alpha   the significance level. Has to be a numeric value between 0 and 1.

intercept   logical. If TRUE, an intercept is included in the outcome model.

B   number of bootstrap samples. Has to be a positive integer value. Bootstrap methods are used to calculate the iv strength threshold if threshold_boot is TRUE and for the violation space selection.

Details

The treatment and outcome models are assumed to be of the following forms:

$$D_i = f(Z_i, X_i) + \delta_i$$

$$Y_i = \beta \cdot D_i + h(Z_i, X_i) + \phi(X_i) + \epsilon_i$$

where $f(Z_i, X_i)$ is estimated using a random forest, $h(Z_i X_i)$ is approximated using the hat matrix weight provided by the user and $\phi(X_i)$ is approximated by a linear combination of the columns in W. The errors are allowed to be heteroscedastic. $A1$ is used to perform violation space selection and

to estimate the treatment effect.

The violation space candidates should be in a nested sequence as the violation space selection is performed by comparing the treatment estimate obtained by each violation space candidate with the estimates of all violation space candidates further down the list vio_space that provide enough IV strength. Only if no significant difference was found in all of those comparisons, the violation space candidate will be selected. If sel_method is 'comparison', the treatment effect estimate of this violation space candidate will be returned. If sel_method is 'conservative', the treatment effect estimate of the successive violation space candidate will be returned provided that the IV strength is large enough. The specification of suitable violation space candidates is a crucial step because a poor approximation of $g(Z_i, X_i)$ might not address the bias caused by the violation of the IV assumption sufficiently well. The function create_monomials can be used to create a predefined sequence of violation space candidates consisting of monomials. The function create_interactions can be used to create a predefined sequence of violation space candidates consisting of two-way interactions between the instrumens themselves and between the instruments and the instruments and baseline covariates.

The instrumental variable(s) are considered strong enough for violation space candidate V_q if the estimated IV strength using this violation space candidate is larger than the obtained value of the threshold of the IV strength. The formula of the threshold of the IV strength has the form $\min\{\max\{2\cdot\mathrm{Trace}[\mathrm{M}(V_q)], \mathrm{iv\_threshold}\}+S(V_q), 40\}$ if threshold_boot is TRUE, and $\min\{\max\{2\cdot\mathrm{Trace}[\mathrm{M}(V_q)], \mathrm{iv\_threshold}\}, 40\}$ if threshold_boot is FALSE. The matrix $\mathrm{M}(V_q)$ depends on the hat matrix obtained from estimating $f(Z_i, X_i)$, the violation space candidate V_q and the variables to include in the outcome model W. $S(V_q)$ is obtained using a bootstrap and aims to adjust for the estimation error of the IV strength. Usually, the value of the threshold of the IV strength obtained using the bootstrap approach is larger. Thus, using threshold_boot equals TRUE leads to a more conservative IV strength test. For more information see subsection 3.3 in Guo and Buehlmann (2022).

See also Carl et al. (2023) for more details.

Value

A list containing the following elements:

Coef_all a series of point estimates of the treatment effect obtained by the different violation space candidates.

sd_all standard errors of the estimates of the treatmnet effect obtained by the different violation space candidates.

pval_all p-values of the treatment effect estimates obtained by the different violation space candidates.

CI_all confidence intervals for the treatment effect obtained by the different violation space candidates.

Coef_sel the point estimator of the treatment effect obtained by the selected violation space candidate(s).

sd_sel the standard error of Coef_sel.

pval_sel p-value of the treatment effect estimate obtained by the selected violation space candidate(s).

CI_sel confidence interval for the treatment effect obtained by the selected violation space candidate(s).

iv_str IV strength using the different violation space candidates.

iv_thol the threshold for the IV strength using the different violation space candidates.

Qmax the violation space candidate that was the largest violation space candidate for which the IV strength was considered large enough determined by the IV strength test. If 0, the IV Strength test failed for the first violation space candidate. Otherwise, violation space selection was performed.

q_comp the violation space candidate that was selected by the comparison method over the multiple data splits.

q_cons the violation space candidate that was selected by the conservative method over the multiple data splits.

invalidity shows whether the instrumental variable(s) were considered valid, invalid or too weak to test for violations. The instrumental variables are considered too weak to test for violations if the IV strength is already too weak using the first violation space candidate (besides the empty violation space). Testing for violations is always performed by using the comparison method.

References

- Zijian Guo, and Peter Buehlmann. Two Stage Curvature Identification with Machine Learning: Causal Inference with Possibly Invalid Instrumental Variables. *arXiv:2203.12808*, 2022

- Nicolai Meinshausen, Lukas Meier, and Peter Buehlmann. P-values for high-dimensional regression. *Journal of the American Statistical Association*, 104(488):1671-1681, 2009. 16, 18

- Victor Chernozhukov, Denis Chetverikov, Mert Demirer, Esther Duflo, Christian Hansen, Whitney Newey, and James Robins. Double/debiased machine learning for treatment and structural parameters: Double/debiased machine learning. *The Econometrics Journal*, 21(1), 2018. 4, 16, 18

- David Carl, Corinne Emmenegger, Peter Buehlmann, and Zijian Guo. TSCI: two stage curvature identification for causal inference with invalid instruments. *arXiv:2304.00513*, 2023

See Also

tsci_boosting for TSCI with boosting.

tsci_forest for TSCI with random forest.

tsci_poly for TSCI with polynomial basis expansion.

Examples

```
### a small example without baseline covariates
if (require("MASS")) {
  # sample size
```

```
    n <- 100
    # the IV strength
    a <- 1
    # the violation strength
    tau <- 1
    # true effect
    beta <- 1
    # treatment model
    f <- function(x) {1 + a * (x + x^2)}
    # outcome model
    g <- function(x) {1 + tau * x}

    # generate data
    mu_error <- rep(0, 2)
    Cov_error <- matrix(c(1, 0.5, 0.5, 1), 2, 2)
    Error <- MASS::mvrnorm(n, mu_error, Cov_error)
    # instrumental variable
    Z <- rnorm(n)
    # treatment variable
    D <- f(Z) + Error[, 1]
    # outcome variable
    Y <- beta * D + g(Z) + Error[, 2]

    # Two Stage User Defined
    # get hat matrix of treatment model
    A <- cbind(1, Z, Z^2, Z^3)
    weight <- A %*% chol2inv(chol(t(A) %*% A)) %*% t(A)
    # create violation space candidates
    vio_space <- create_monomials(Z, 2, "monomials_main")
    # perform two stage curvature identification
    output_UD <- tsci_secondstage(Y, D, Z, vio_space = vio_space, weight = weight,
                                  B = 100)
    summary(output_UD)
}
```

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